

Time limit: 15 minutes.

Instructions: This tiebreaker contains 3 short answer questions. All answers must be expressed in simplest form unless specified otherwise. You will submit answers to the problem as you solve them, and may solve problems in any order. You will not be informed whether your answer is correct until the end of the tiebreaker. You may submit multiple times for any of the problems, but **only the last submission for a given problem will be graded**. The participant who correctly answers the most problems wins the tiebreaker, with ties broken by the time of the last correct submission.

No calculators.

1. Line segment \overline{AE} of length 17 bisects \overline{DB} at a point C . If $\overline{AB} = 5$, $\overline{BC} = 6$ and $\angle BAC = 78$ degrees, calculate $\angle CDE$.
2. Points A, B, C are chosen on the boundary of a circle with center O so that $\angle BAC$ encloses an arc of 120 degrees. Let D be chosen on \overline{BA} so that $\angle AOD$ is a right angle. Extend \overline{CD} so that it intersects with O again at point P . What is the measure of the arc, in degrees, that is enclosed by $\angle ACP$? Please use the \tan^{-1} function to express your answer.
3. Consider a regular polygon with 2^n sides, for $n \geq 2$, inscribed in a circle of radius 1. Denote the area of this polygon by A_n . Compute

$$\prod_{i=2}^{\infty} \frac{A_i}{A_{i+1}}$$